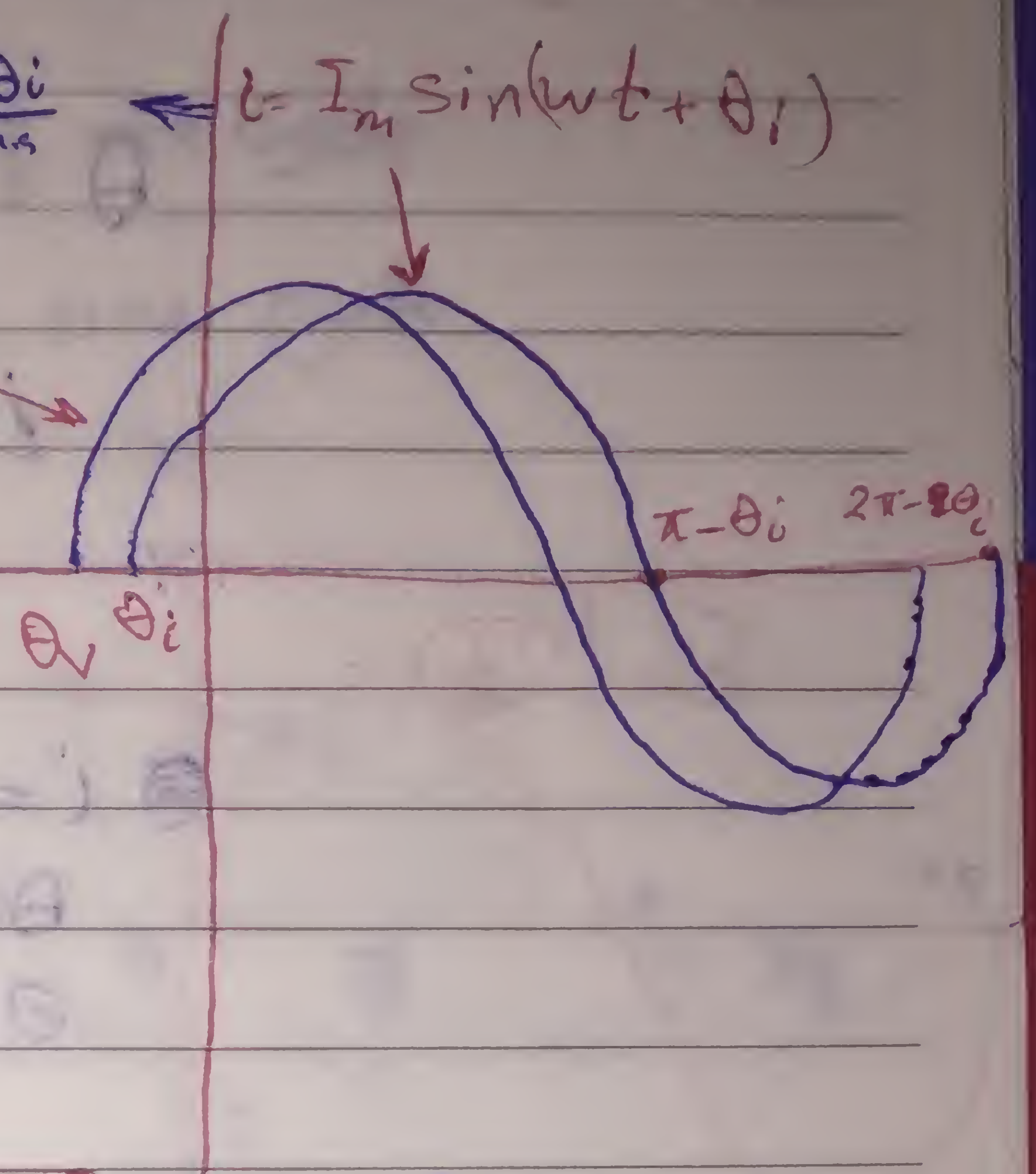


\* phase shift

$$I = \bar{I} \angle \theta_i$$

phasor form  
 $V = \bar{V} = \frac{V_m}{\sqrt{2}} \angle \theta_v$

$$V = V_m \sin(\omega t + \theta_v)$$



$$\theta = \theta_v - \theta_i$$

↓  
 phase  
 angle  
 of  $i, v$

Find phase shift

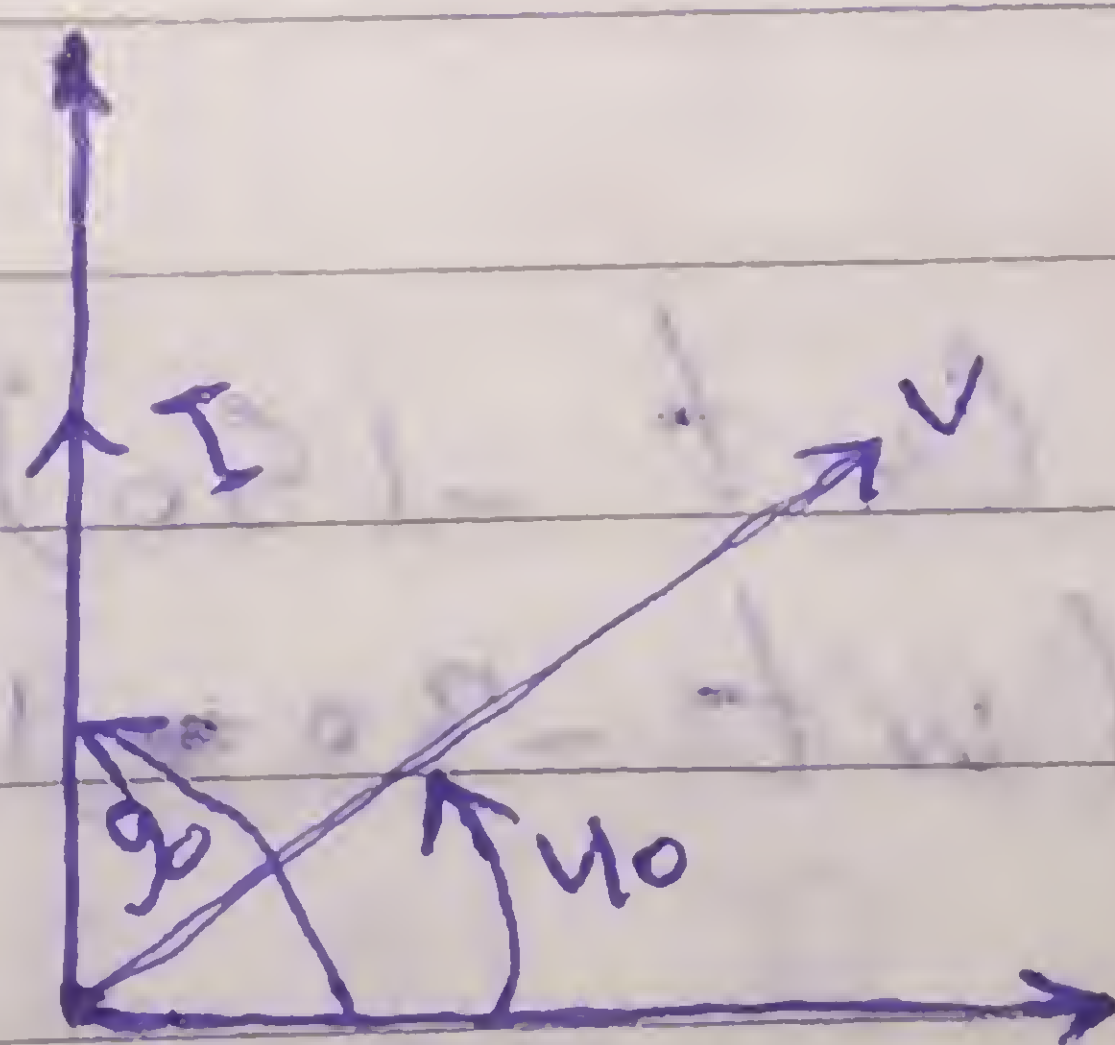
- ①  $v = 100 \sin(\omega t + 40^\circ), i = 10 \sin(\omega t + 90^\circ)$
- ②  $v = 15 \sin(\omega t + 50^\circ), i = 1 \sin(\omega t - 30^\circ)$
- ③  $v = 30 \sin(\omega t - 10^\circ), i = 2 \cos(\omega t + 30^\circ)$
- ④  $v = 20 \sin(\omega t + 10^\circ), i = 5 \sin(\omega t + 30^\circ)$
- ⑤  $v = 30 \sin(\omega t - 180^\circ), i = 5 \cos(\omega t - 30^\circ)$

$v$  lead  $i$  by  $\theta$   
 or  
 $i$  lag  $v$  by  $\theta$

Sol ①:  $\theta_v = 40^\circ, \theta_i = 90^\circ$

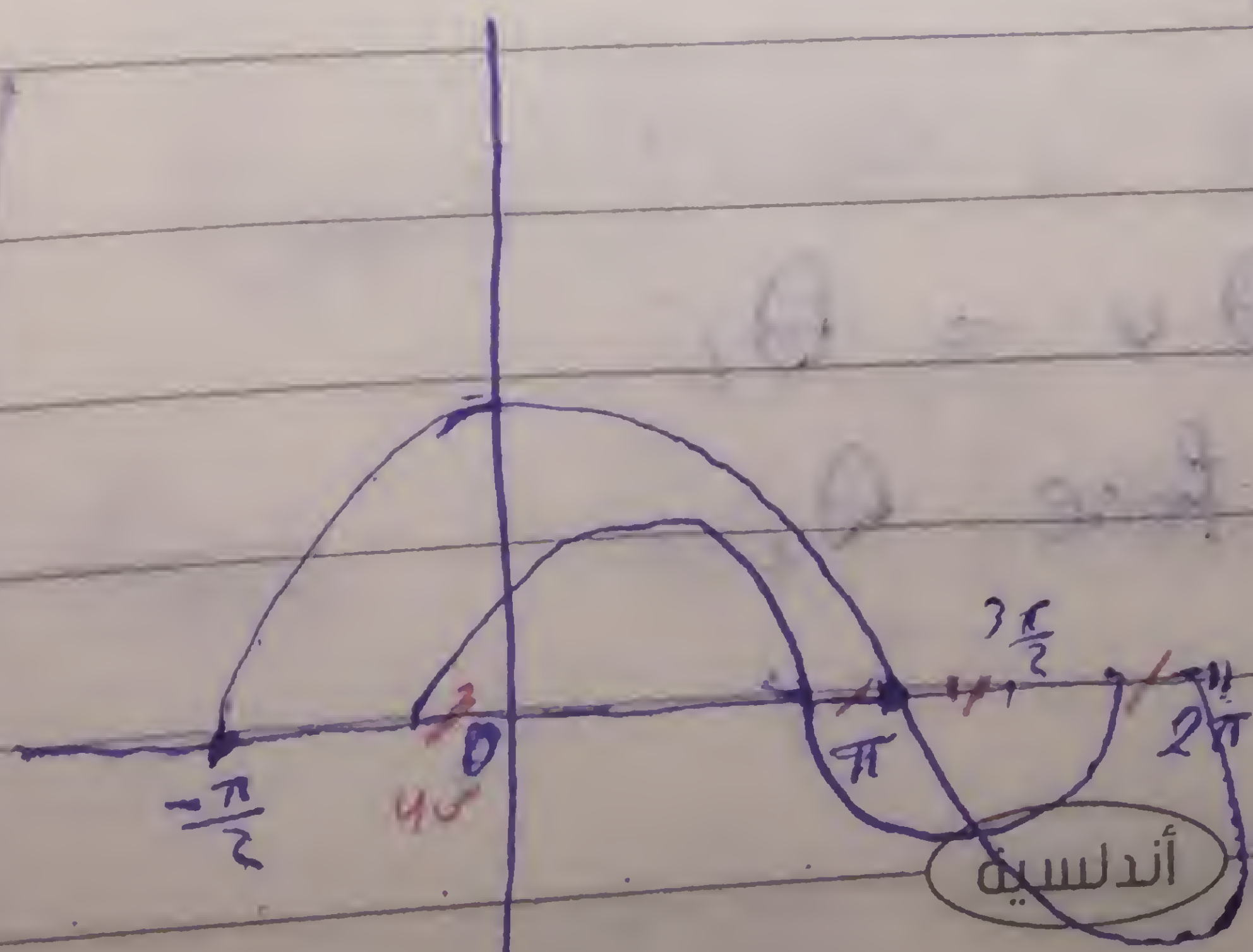
$$\theta = \theta_v - \theta_i = 40^\circ - 90^\circ = -50^\circ$$

$I$  lead  $V$  by  $50^\circ$



scale  
 ندرم بر حسب  
 توان و ولتاژ

"Phasor Diagram"



$$\cos \omega t = \sin(\omega t + 90^\circ)$$

$$\sin \omega t = \cos(\omega t - 90^\circ)$$

$$\sin(-\theta) = -\sin \theta$$

$$\cos(-\theta) = \cos \theta$$

$$-\sin \theta = \sin(\theta \pm 180^\circ)$$

$$-\cos \theta = \cos(\theta \pm 180^\circ)$$



Sol ② -  $\theta_v = 50^\circ$  &  $\theta_i = -30^\circ$

$$\theta = 50 + 30 = 80$$

i lag v by  $80^\circ$

Sol ③:-

$$i = 2 \sin(\omega t + 90 + 10)$$

$$\theta_v = -10$$

$$\theta_i = 100$$

$$\theta = -110$$

i lead v by  $110^\circ$

Sol ④:-

ای نوسان اولی صغیر

$$i = \sin(\omega t + 30 - 180)$$

$$\theta_v = 10 \text{ or } \theta_i = -150$$

$$\theta = -160$$

v lead i  $160^\circ$  or  $\theta_v - \theta_i = \theta$

Sol ⑤:-

$$v = 30 \sin(\omega t - 150)$$

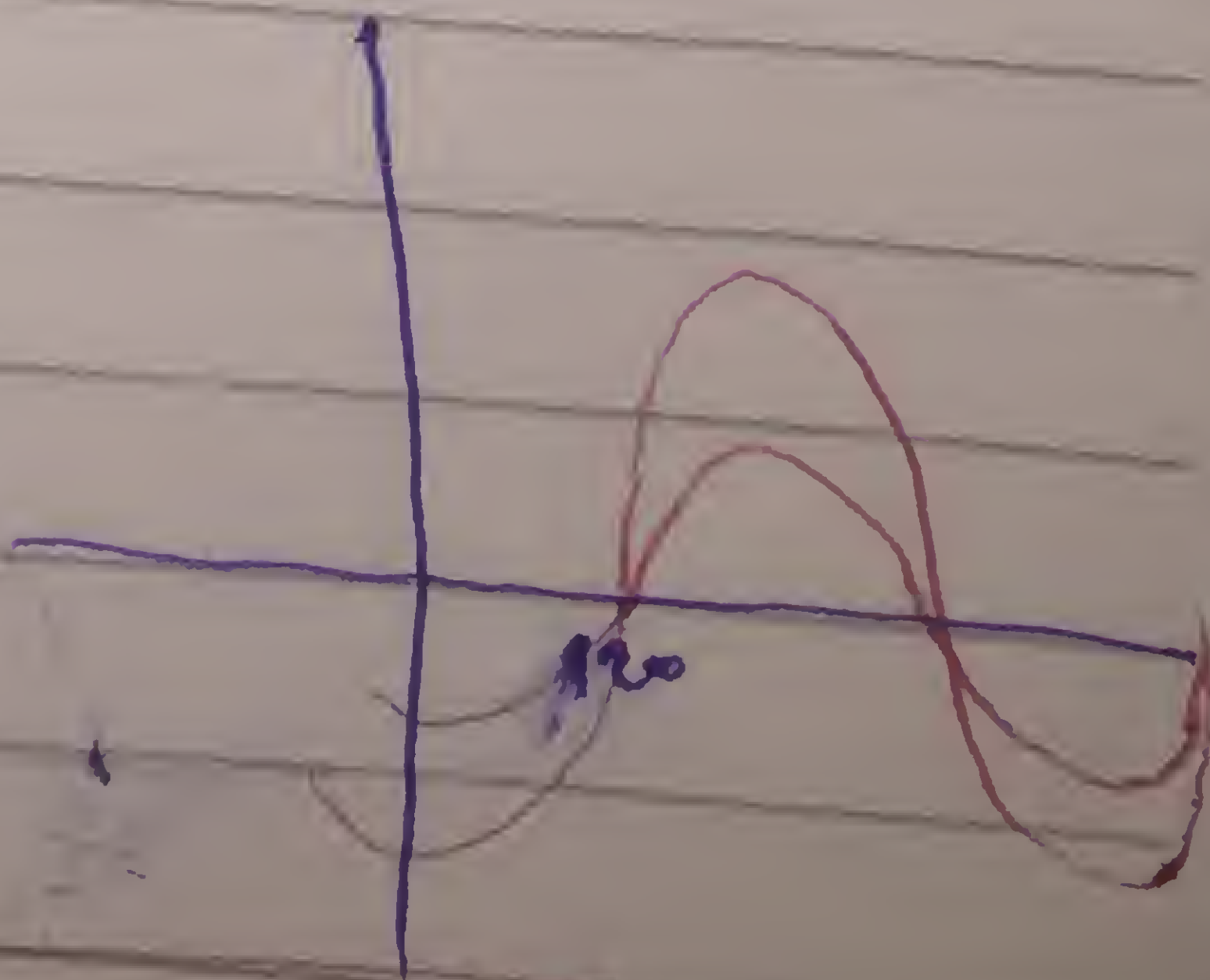
$$i = 5 \cos(\omega t - 30 - 180 + 90)$$

$$\theta_v = -150$$

$$\theta_i = -180$$

$$\theta_v = \theta_i$$

$\theta_v$  lags  $\theta_i$





Subject.

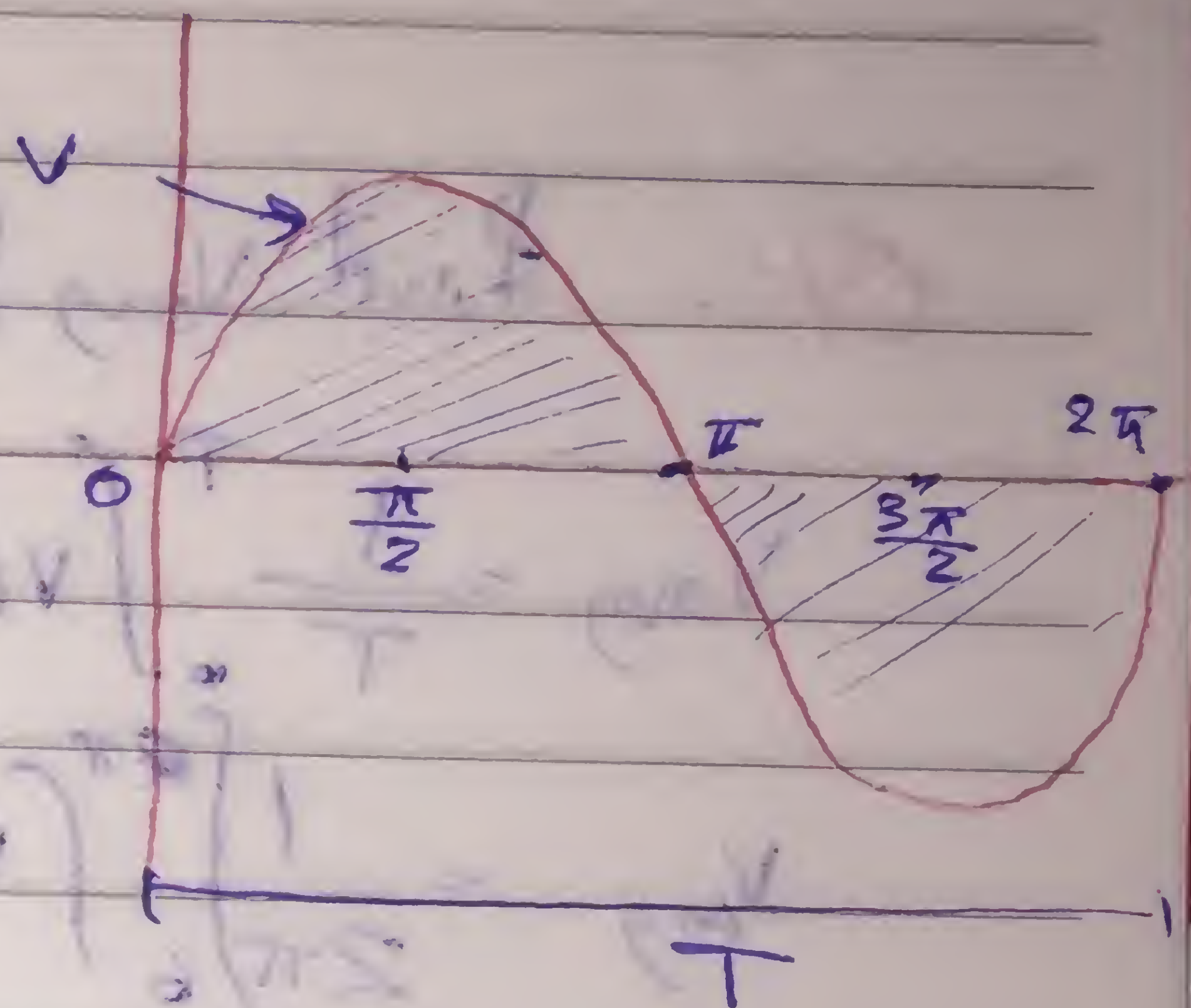
Date.

\* Average value or Mean value :-

$$V_{Avg} = \frac{\Sigma \text{Area under the curve of one cycle}}{\text{Length of curve of one cycle}}$$

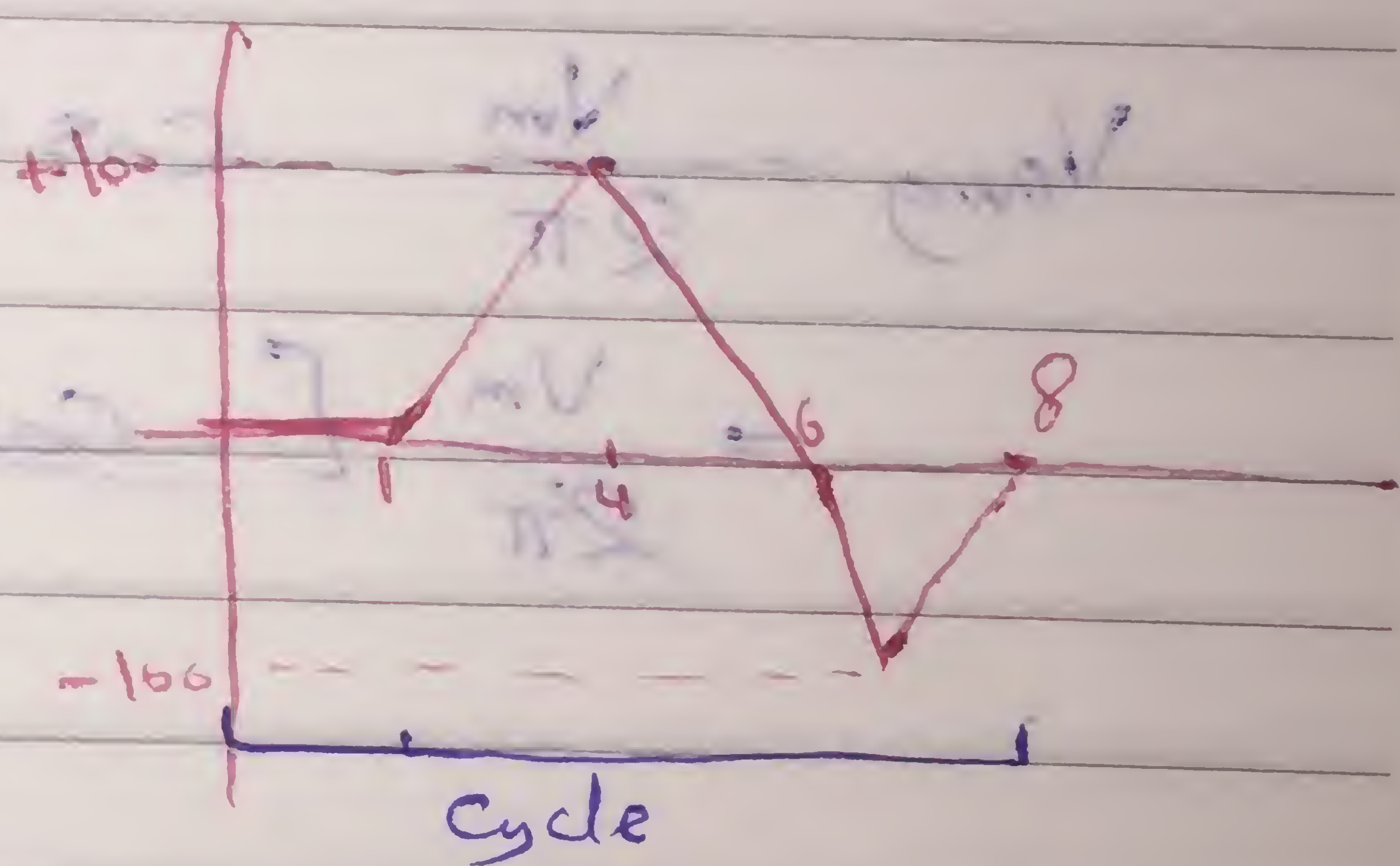
$$V_{avg} = \frac{1}{T} \int_0^T v(t) dt$$

$$= \frac{1}{2\pi} \int_0^{2\pi} V_m \sin \omega t d\omega t$$



ex. Find the  $V_{avg}$ .

$$V_{avg} = \frac{\frac{5}{2} \times 100 - \frac{2}{3} \times 100}{7}$$



\* Effective value or Root mean Square value:

$$V_{eff} \text{ or } V_{r.m.s} \text{ or } V_{avg}$$

$$I_{dc} \Rightarrow P = I_{dc}^2 R$$

$$P_{(t)} = i^2 R = I_m^2 \sin^2(\omega t) \cdot R$$

$$P_{avg} = \frac{1}{T} \int_0^T P dt = \frac{1}{T} \int_0^T I_{dc}^2 R dt$$



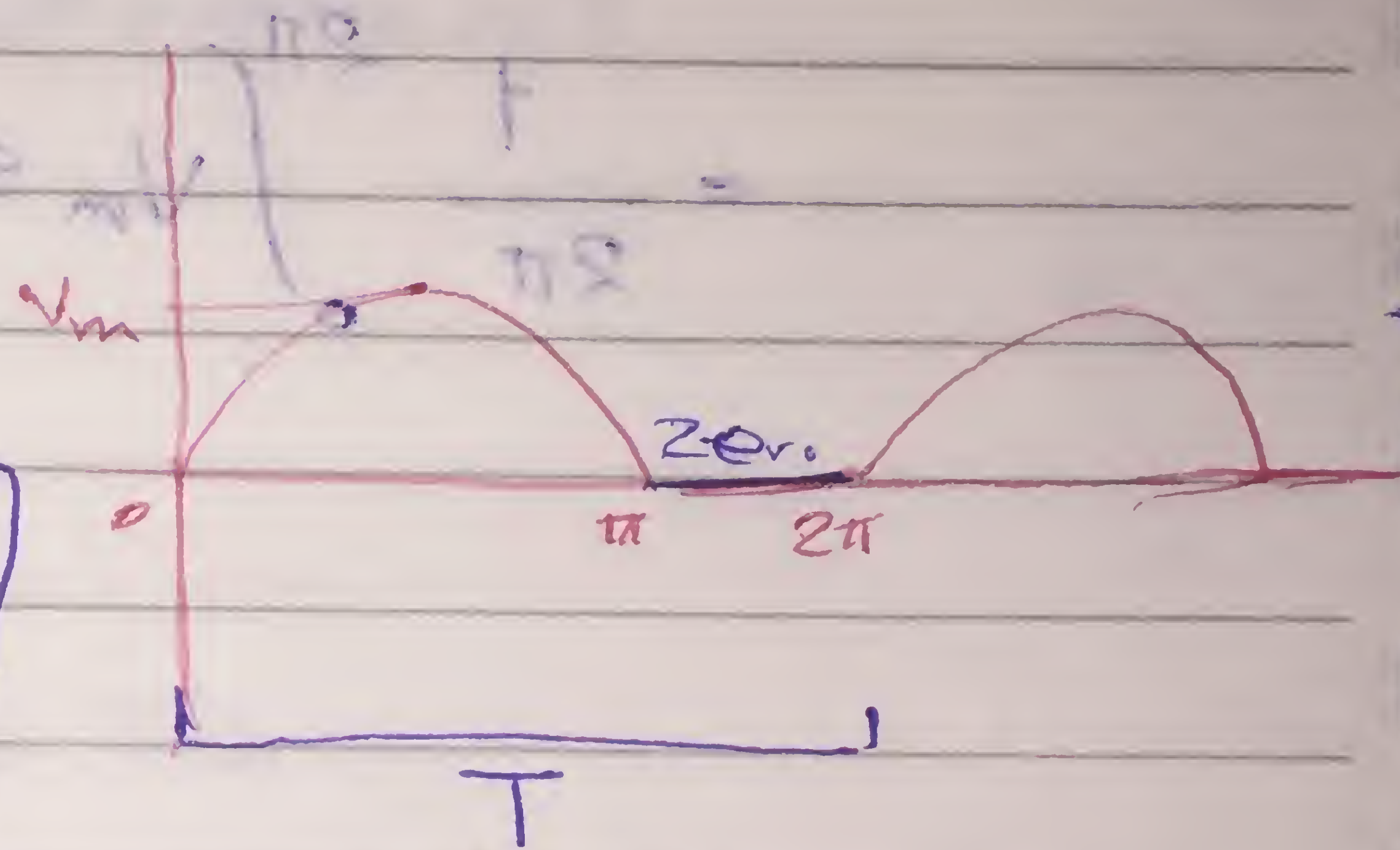
$$I_{eff} = \sqrt{\frac{1}{T} \int_0^T i^2(t) dt}$$

$$V_{eff} = V_{r.m.s} = V = \sqrt{\frac{1}{T} \int_0^T v^2(t) dt}$$

Ex:- Find  $V_{avg}$  &  $V_{eff}$

$$V_{avg} = \frac{1}{T} \int_0^T v(t) dt$$

$$V_{avg} = \frac{1}{2\pi} \int_0^{2\pi} V_m \sin \omega t d\omega t$$



$$V_{avg} = \frac{V_m}{2\pi} \left[ -\cos \omega t \right]_0^{2\pi}$$

$$= \frac{V_m}{2\pi} [-\cos 2\pi + \cos 0] = \frac{V_m}{2\pi} [-1 + 1] = 0$$

$$V_{eff} = \sqrt{\frac{1}{2\pi} \int_0^{2\pi} V_m^2 \sin^2(\omega t) d\omega t}$$

$$= \sqrt{\frac{V_m^2}{2\pi} \int_0^{2\pi} \sin^2(\omega t) d\omega t}$$

$$= \sqrt{\frac{V_m^2}{2\pi} \int_0^{2\pi} (1 - \cos 2\omega t) d\omega t}$$



Subject.

Date.

Report: Sin wave find  $V_{eff}$  &  $V_{avg}$   
(2016)

$$\frac{V_{max}}{\sqrt{2}}$$